

# Commutative Ring Theory Days 2010

May 19-20-21, 2010

Roma, Italy

## AMALGAMATED ALGEBRAS ALONG AN IDEAL

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[Joint work with M. D'Anna and M. Fontana]. Let  $f : A \rightarrow B$  be a ring homomorphism and  $J$  be an ideal of  $B$ . Then we consider the following subring

$$A \rtimes^f J := \{(a, f(a) + j) : a \in A, j \in J\}$$

of  $A \times B$  and call it *the amalgamation of  $A$  with  $B$  along  $J$ , with respect to  $f$* . This construction generalizes the amalgamated duplication of a ring along an ideal, introduced and studied in [1] and [2]. Moreover, several constructions (like the rings of the type  $A + XB[X]$  or  $D + M$ , etc.) can be seen as particular cases of the amalgamation. In this talk, I will study conditions on  $A, B, f$  and  $J$  to transfer algebraic properties from  $A$  and  $B$  to  $A \rtimes^f J$  and conversely, by using also the fiber product structure of  $A \rtimes^f J$ . I will give a classification of all the fiber products that can arise from an amalgamation. Moreover I will study the chains of prime ideals of  $A \rtimes^f J$  in order to give bounds for the dimension of  $A \rtimes^f J$ .

- [1 ] M.D'Anna and M. Fontana *An amalgamated duplication of a ring along an ideal: the basic properties*, J. Algebra Appl. **6** (2007), pp. 443–459.
- [2 ] M.D'Anna and M. Fontana, *The amalgamated duplication of a ring along a multiplicative-canonical ideal*, Arkiv Mat. **45** (2007), pp. 241–252.

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